

Multi-body NRSfM (NRSfM Challenge 2017)

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- 1 Introduction
- 2 Spatial-Temporal Representation
- 3 Joint Optimization Formulation
- 4 Experiments and Results

Introduction

Why Multi-body NRSfM Representation?

- Real-world scene consist of multiple deforming objects. For example: pedestrians, soccer match, human interaction and etc.

Goal:

- To segment and reconstruct multiple deforming objects in a scene, **simultaneously**.

Baseline strategy:

- Two-stage approach:
 - motion segmentation followed by non-rigid reconstruction
 - non-rigid reconstruction followed by motion segmentation.

Why unified approach?

- To better exploit the inherent structure of the problem
 - ⇒ Motion segmentation benefits reconstruction
 - ⇒ Reconstruction benefits motion segmentation
- Both tasks can be solved efficiently within a single optimization.
- Computationally and numerically efficient.

Spatial-Temporal Representation

To exploit the intrinsic structure both spatially and temporally, we propose the spatial-temporal representation for complex non-rigid reconstruction.

- Spatial Clustering \Rightarrow Provides motion segmentation cues
- Temporal Clustering \Rightarrow Benefits 3D reconstruction
- Spatial Clustering exploits **Trajectory space**.
- Temporal Clustering exploits **Shape space**.

Trajectory Space

Classical NRSfM Representation

$$\mathbf{W} = \mathbf{RS}, \text{ where } \mathbf{R} \in \mathbb{R}^{2F \times 3F}, \mathbf{S} \in \mathbb{R}^{3F \times P} \quad (1)$$

$\mathbf{W} \in \mathbb{R}^{2F \times P} \Rightarrow$ Measurement matrix.

$\mathbf{S} \Rightarrow$ Shape matrix.

$\mathbf{R} \Rightarrow$ Rotation matrix (Orthographic Camera Model).

Trajectory Space

Representation of multiple non-rigid deformation in the trajectory space.

$$S = SC_1, \text{diag}(C_1) = 0, 1^T C_1 = 1^T.$$

$$S \in \mathbb{R}^{3F \times P}, C_1 \in \mathbb{R}^{P \times P}.$$

(2)

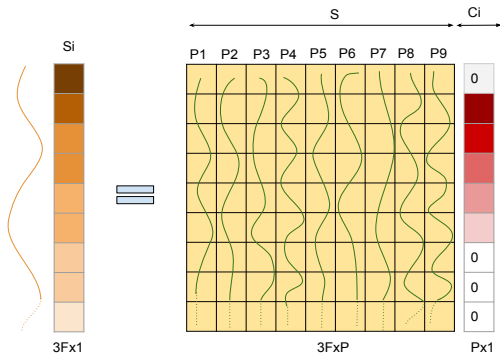


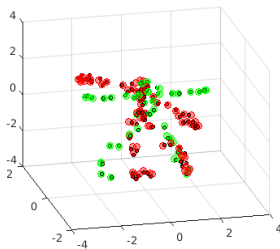
Figure: Illustration of trajectory space

Shape Space

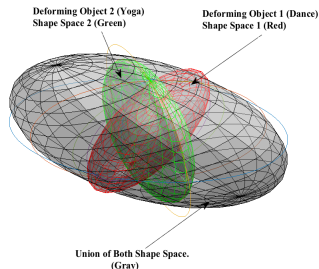
Representation of multiple non-rigid deformation in the shape space.

$$\begin{aligned} S^\sharp &= S^\sharp C_2, \text{diag}(C_2) = 0, 1^T C_2 = 1^T. \\ S^\sharp &\in \mathbb{R}^{3P \times F}, C_2 \in \mathbb{R}^{F \times F}. \end{aligned} \quad (3)$$

⇒ Intuition [Cluster distinct activity (Ex: Dance, Yoga)]



(a)



(b)

Visual illustration

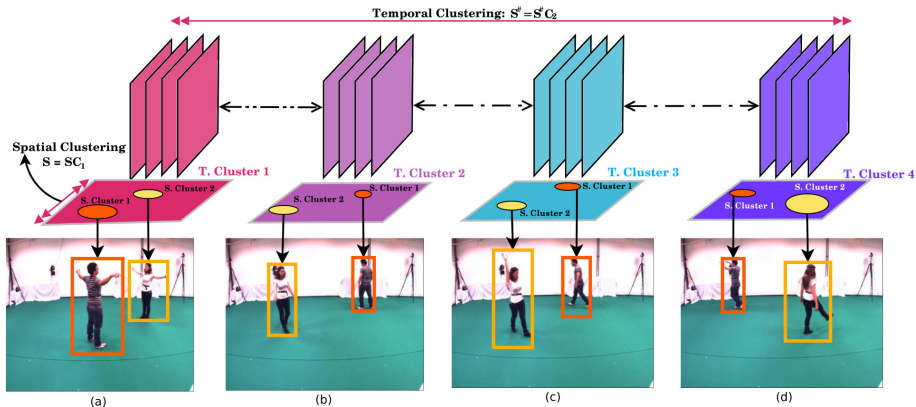


Figure: Intuition of spatial-temporal clustering.

Joint Optimization Formulation

- Objective from the **trajectory space**

$$\begin{aligned} & \underset{C_1}{\text{minimize}} \quad \lambda_1 \|C_1\|_1 + \frac{(1 - \lambda_1)}{2} \|C_1\|_F^2 \\ & \text{subject to:} \\ & S = SC_1, \text{diag}(C_1) = 0, 1^T C_1 = 1^T, \lambda_1 \in [0, 1]. \end{aligned} \tag{4}$$

- Objective from the **shape space**

$$\begin{aligned} & \underset{C_2}{\text{minimize}} \quad \lambda_3 \|C_2\|_1 + \frac{(1 - \lambda_3)}{2} \|C_2\|_F^2 \\ & \text{subject to:} \\ & S^\# = S^\# C_2, \text{diag}(C_2) = 0, 1^T C_2 = 1^T, \lambda_3 \in [0, 1]. \end{aligned} \tag{5}$$

Joint Optimization Formulation

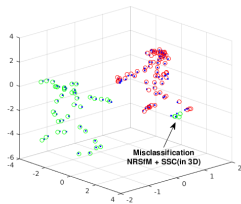
- Overall Objective \Rightarrow solved using ADMM

$$\begin{aligned} & \underset{S, C_1, C_2}{\text{minimize}} \quad \frac{1}{2} \|W - RS\|_F^2 + \lambda_1 \|C_1\|_1 + \frac{1 - \lambda_1}{2} \|C_1\|_F^2 + \lambda_2 \|S^\# \|_* + \\ & \lambda_3 \|C_2\|_1 + \frac{1 - \lambda_3}{2} \|C_2\|_F^2. \\ & \text{subject to:} \\ & S = SC_1, S^\# = S^\# C_2, \\ & \mathbf{1}^T C_1 = \mathbf{1}^T, \mathbf{1}^T C_2 = \mathbf{1}^T, \\ & \text{diag}(C_1) = 0, \text{diag}(C_2) = 0, \\ & \lambda_1, \lambda_3 \in [0, 1]. \end{aligned} \tag{6}$$

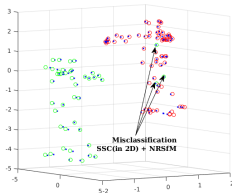
where $S^\# \in \mathbb{R}^{3P \times F}$, $C_1 \in \mathbb{R}^{P \times P}$, and $C_2 \in \mathbb{R}^{F \times F}$ and $\lambda_1, \lambda_2, \lambda_3$ are the trade-off parameters.

Experiments and Results

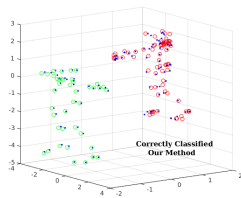
- Advantage over two stage approach



(a) NRSfM \Rightarrow SSC [2]



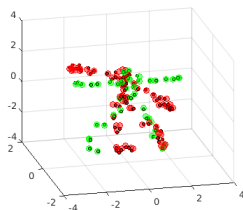
(b) SSC [2] \Rightarrow NRSfM



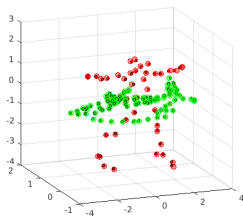
(c) Our approach

Qualitative results on synthetic sequence

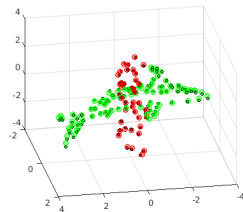
- Two deforming objects are intersecting each other.



(d) Dance-Yoga



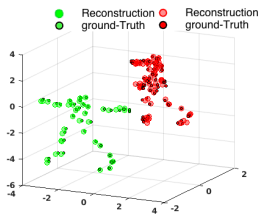
(e) Shark-Stretch



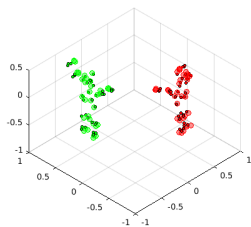
(f) Shark-Yoga

Qualitative results(Cont.)

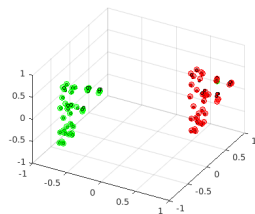
- Two deforming objects are well separated in space.



(g) Dance-Yoga



(h) UMPM p3_ball_1



(i) UMPM p4_meet_12

UMPM dataset [10] is composed of real-image tracks.

Quantitative Results on benchmark real-dataset

Datasets	BMM[1]	PND[9]	Zhu et al.[11]	Kumar et al.[8]	Ours
p2_free_2	0.1973	0.1544	0.1142	0.1992	0.1171
p2_grab_2	0.2018	0.1570	0.0960	0.2080	0.0822
p3_ball_1	0.1356	0.1477	0.0832	0.1348	0.0810
p4_meet_12	0.0802	0.0862	0.0972	0.0821	0.0815
p4_table_12	0.2313	0.1588	0.1322	0.2313	0.0994

Table: Performance comparison on real benchmark UMPM dataset [10] (showing relative 3D reconstruction error).

Quantitative Results on benchmark real-dataset

Datasets	BMM[1]	PND[9]	Zhu et al.[11]	Kumar et al.[8]	Ours
Face Seq.1	0.078	0.077	0.082	0.075	0.073
Face Seq.2	0.059	0.062	0.063	0.050	0.052
Face Seq.3	0.042	0.051	0.057	0.038	0.039
Face Seq.4	0.049	0.041	0.056	0.044	0.040

Table: Performance comparison on real benchmark dense face dataset [3] (showing relative 3D reconstruction error).

Evaluation result on NRSfM challenge dataset for test frame.

- Mean RMS (in mm) for orthogonal category.

Datasets	Articulated	Balloon	Paper	Stretch	Tearing
Our Method	10.15	10.64	15.78	9.96	14.17

Table: Performance on the NRSfM challenge dataset on all provided sequence for *single* test image provided by the challenge organizers.

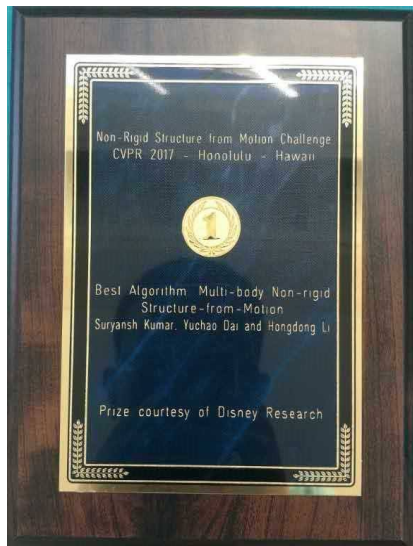
- Note: We submitted results for two methods. Numerically, both of them performed with similar reconstruction accuracy [8] [7].

Performance comparison with other top 3 performing algorithms on NRSfM challenge dataset.

- Mean RMS (in mm) for orthogonal category.

Datasets	Articulated	Balloon	Paper	Stretch	Tearing	Mean
Multibody [7]	45.51	14.55	22.88	18.30	21.98	24.64
CSF2 [5]	35.51	19.01	33.95	23.22	18.77	26.09
RIKS [6]	42.11	18.45	32.18	22.88	18.12	26.75
KSTA [4]	36.63	24.88	31.96	24.25	17.59	26.86

Table: Note: These evaluations were done by the organizers of NRSfM challenge at CVPR 2017.



Thanks

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